## Discrete Morse theory erratum

This page is devoted to errors and typos in the book Discrete Morse Theory, published by AMS press, 2019.

$\mathbf{page}$	line	Comments
69	-10	The word "increasing" should be "decreasing."
71	-4	The object $W$ induced by the generalized discrete Morse function $f$ should have a different name than "generalized discrete vector field" defined in the middle of page 71. Call the $W$ induced by $f$ a <b>generalized gradient.</b> This is the object to which we refer in Corollary 4.30 (see the line in p. 116 below)
98	24	$\operatorname{null}(\partial_p) - \operatorname{rank}(\partial_p) = \operatorname{null}(\partial'_p) - \operatorname{rank}(\partial'_p) \text{ should be}$ $\operatorname{null}(\partial_p) - \operatorname{rank}(\partial_{p+1}) = \operatorname{null}(\partial'_p) - \operatorname{rank}(\partial'_{p+1})$
102	11	the inequality is reversed. It should read $b_i \leq m_i$ .
105	-10	"is" should be "in"
107	8	$ au$ is critical, not $\gamma$
107	-2	$f_t$ should be $h_t$
116	-5	"generalized discrete vector field" should be called "generalized gradient" to imply it is induced by a generalized discrete Morse function (see the line on p. 71 above)
119	-3	In definition 5.5, last line, the roles of $k$ and $i$ are switched.
121	-3	$\sigma_p$ should be $\sigma^{(p)}$
141	6	The definition of $K(\alpha)$ is wrong. The $K(\alpha)$ should be defined as the smallest subcomplex of K containing all $\beta$ such that $\beta \preceq \alpha$ .
150	Ex 6.4	Assume $n > 1$
153	Ex 6.10	$x_4$ should be $x_0$ in the diagram
153	Prob 6.12	Assume $n > 0$
166	Lemma 6.34	$link_{\Delta^n}(v)$ should be $link_M(v)$
176	Prob 7.10	G should be $K$
181		In both Prob 7.21 and Prob 7.22, $G$ should be $T$
194	15	It should read $f(\tilde{\sigma}_i) \leq f(\tau) \leq f(\sigma_i)$

199	16	$V \circ V$ should be $V \circ \partial$
201	-3	$k_p^{\infty}$ should be $k_p^{\Phi}$
203- 206		The matrix on p 203, 204, and 206 should be transposed.
218	Alg 5	Line 5 should be executed after the for clause in line 3, and thus its indentation should be the same as the one of the "for" clause. The "endfor" in line 9 should be placed after line 5.